4.2. Image Compression -- JPEG

Overview of JPEG
Major Steps
A Glance at the JPEG Bitstream
Four JPEG Modes
JPEG 2000

Reference: W.B. Pennebaker, J.L. Mitchell, "The JPEG Still Image Data Compression Standard", Van Nostrand Reinhold, 1993.

4.2.1. Overview of JPEG

What is JPEG?

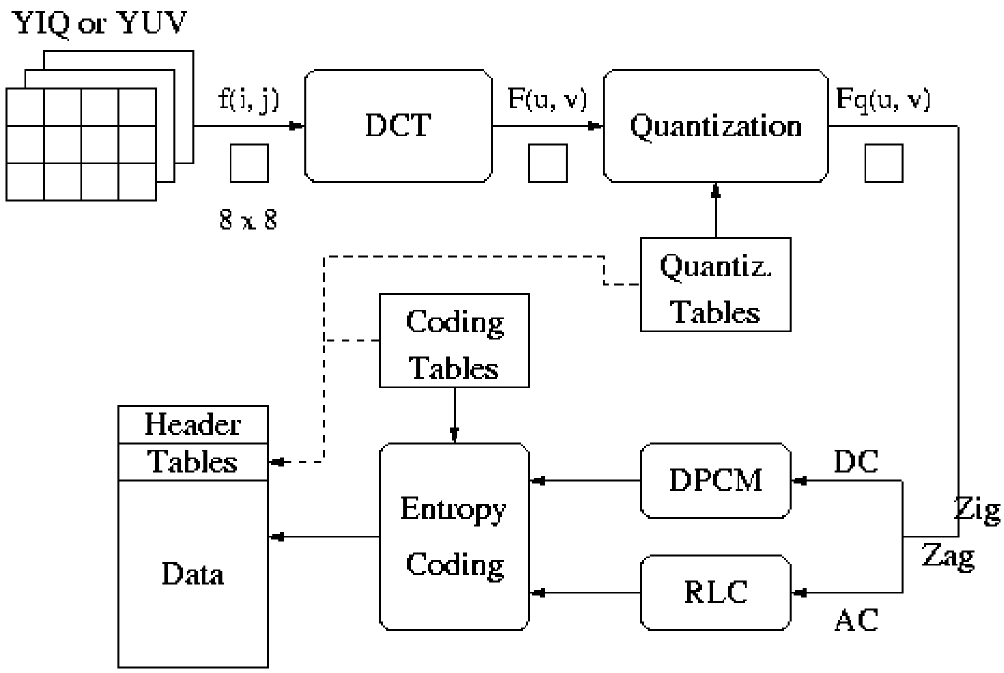
- "Joint Photographic Expert Group". Voted as international standard in 1992.
- Works with color and grayscale images, e.g., satellite, medical, ...

Motivation

- The *compression ratio* of lossless methods (e.g., Huffman, Arithmetic, LZW) is not high enough for image and video compression, especially when the distribution of pixel values is relatively flat.

JPEG overview

- Encoding



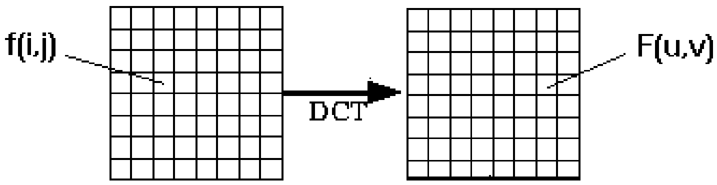
- Decoding -- Reverse the order

4.2.2. Major Steps

- DCT (Discrete Cosine Transformation)
- Quantization
- Zigzag Scan
- DPCM on DC component
- RLE on AC Components
- Entropy Coding

1. Discrete Cosine Transform (DCT)

- From spatial domain to frequency domain:



- **DEFINITIONS**

Discrete Cosine Transform (DCT):

$$F(u,v) = \frac{\Lambda(u)\Lambda(v)}{4} \sum_{i=0}^{7}\sum_{j=0}^{7} \cos\frac{(2i+1)\cdot u\pi}{16} \cdot \cos\frac{(2j+1)\cdot v\pi}{16} \cdot f(i,j)$$

$$\Lambda(\xi) = \begin{cases} \frac{1}{\sqrt{2}} & for\ \xi = 0 \\ 1 & otherwise \end{cases}$$

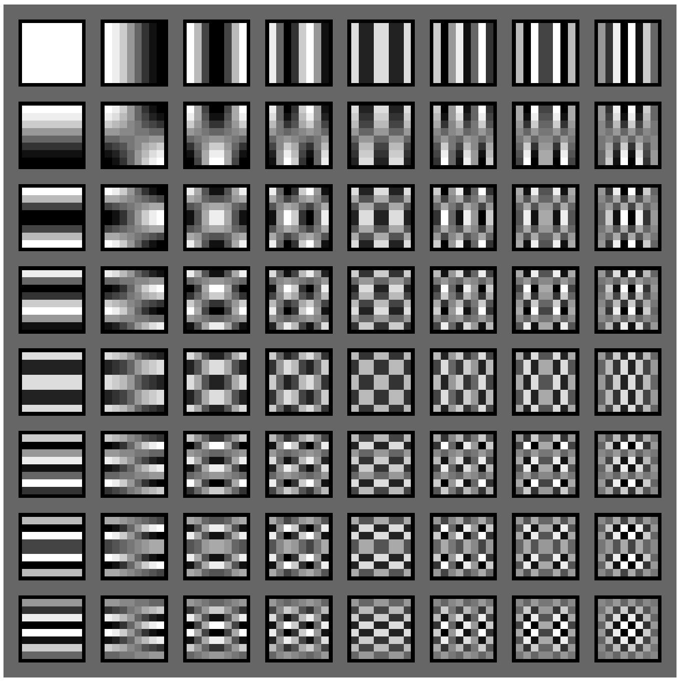
Inverse Discrete Cosine Transform (IDCT):

$$\tilde{f}(i,j) = \frac{1}{4} \sum_{u=0}^{7}\sum_{v=0}^{7} \Lambda(u)\Lambda(v) \cos\frac{(2i+1)\cdot u\pi}{16} \cdot \cos\frac{(2j+1)\cdot v\pi}{16} \cdot F(u,v)$$

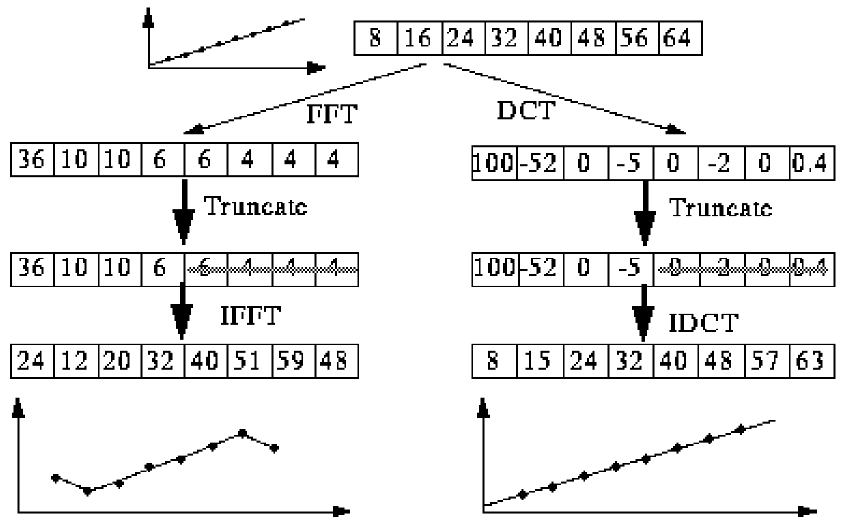
$$\Lambda(\xi) = \begin{cases} \frac{1}{\sqrt{2}} & for\ \xi = 0 \\ 1 & otherwise \end{cases}$$

Question: What are the DC and AC components, e.g., what is F[0,0]?

- The 64 (8 x 8) DCT basis functions:



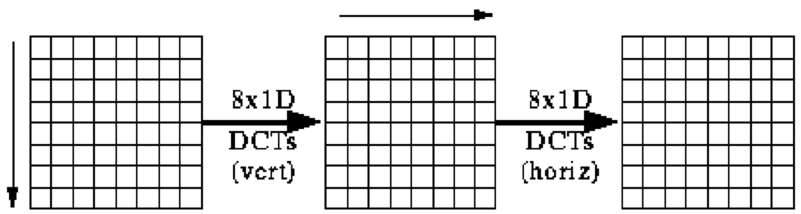
- Why DCT not FFT? -- DCT is like FFT, but can approximate linear signals well with few coefficients.



- Computing the DCT
  - Factoring reduces problem to a series of 1D DCTs:

$$F[u,v] = \frac{1}{2}\sum_i A(u)\cos\frac{(2i+1)u\pi}{16} G[i,v]$$

$$G[i,v] = \frac{1}{2}\sum_j A(v)\cos\frac{(2j+1)v\pi}{16} f[i,j]$$



  - Most software implementations use fixed point arithmetic. Some fast implementations approximate coefficients so all multiplies are shifts and adds.

2. Quantization

- F'[u, v] = round (F[u, v] / q[u, v]).

  Why? -- To reduce number of bits per sample

  Example: 101101 = 45 (6 bits).
  q[u, v] = 4 --> Truncate to 4 bits: 1011 = 11.

- Quantization error is the main source of the Lossy Compression.

Uniform Quantization

- Each F[u,v] is divided by the same constant *N*.

Non-uniform Quantization -- Quantization Tables

- Eye is most sensitive to low frequencies (upper left corner), less sensitive to high frequencies (lower right corner)

- The *Luminance Quantization Table* q(u, v)

16	11	10	16	24	40	51	61
12	12	14	19	26	58	60	55
14	13	16	24	40	57	69	56
14	17	22	29	51	87	80	62
18	22	37	56	68	109	103	77
24	35	55	64	81	104	113	92
49	64	78	87	103	121	120	101
72	92	95	98	112	100	103	99

The *Chrominance Quantization Table* q(u, v)

17	18	24	47	99	99	99	99
18	21	26	66	99	99	99	99
24	26	56	99	99	99	99	99
47	66	99	99	99	99	99	99
99	99	99	99	99	99	99	99
99	99	99	99	99	99	99	99
99	99	99	99	99	99	99	99
99	99	99	99	99	99	99	99

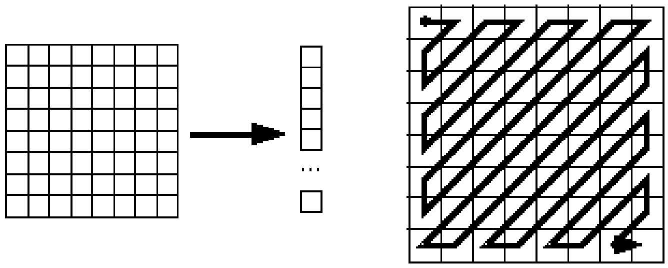
The numbers in the above quantization tables can be scaled up (or down) to adjust the so called *quality factor*.

Custom quantization tables can also be put in image/scan header.

3. Zig-zag Scan

- Why? -- to group low frequency coefficients in top of vector.

- Maps 8 x 8 to a 1 x 64 vector



4. Differential Pulse Code Modulation (DPCM) on DC component

- DC component is large and varied, but often close to previous value.

- Encode the difference from previous 8 x 8 blocks -- DPCM

5. Run Length Encode (RLE) on AC components

- 1 x 64 vector has lots of zeros in it

- Keeps *skip* and *value*, where *skip* is the number of zeros and *value* is the next non-zero component.
- Send (0,0) as end-of-block sentinel value.

6. Entropy Coding

- Categorize DC values into SIZE (number of bits needed to represent) and actual bits.

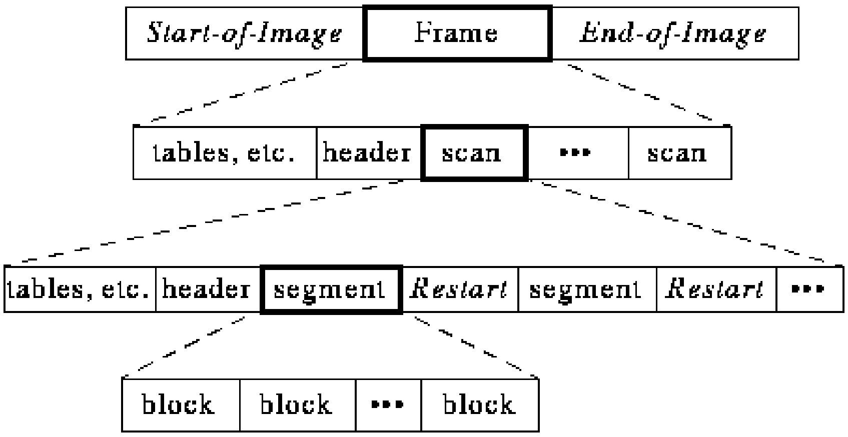
```
------------------------------------
   SIZE              Value
------------------------------------
    1                -1, 1
    2            -3, -2, 2, 3
    3            -7..-4, 4..7
    4           -15..-8, 8..15
    .                  .
    .                  .
    .                  .
   10       -1023..-512, 512..1023
------------------------------------
```

  Example: if DC value is 4, 3 bits are needed.

  Send off SIZE as Huffman symbol, followed by actual 3 bits.

- For AC components two symbols are used: Symbol_1: (*skip, SIZE*), Symbol_2: actual bits. Symbol_1 (*skip, SIZE*) is encoded using the Huffman coding, Symbol_2 is not encoded.
- Huffman Tables can be custom (sent in header) or default.

4.2.3. A Glance at the JPEG Bitstream



- A "Frame" is a picture, a "scan" is a pass through the pixels (e.g., the red component), a "segment" is a group of blocks, a "block" is an 8 x 8 group of pixels.

- Frame header:
  sample precision
  (width, height) of image
  number of components
  unique ID (for each component)
  horizontal/vertical sampling factors (for each component)
  quantization table to use (for each component)

- Scan header
  Number of components in scan
  component ID (for each component)
  Huffman table for each component (for each component)

- Misc. (can occur between headers)
  Quantization tables
  Huffman Tables
  Arithmetic Coding Tables
  Comments
  Application Data

4.2.4. Four JPEG Modes

- Sequential Mode
- Lossless Mode
- Progressive Mode
- Hierarchical Mode

  ** In "Motion JPEG", Sequential JPEG is applied to each image in a video.

1. Sequential Mode

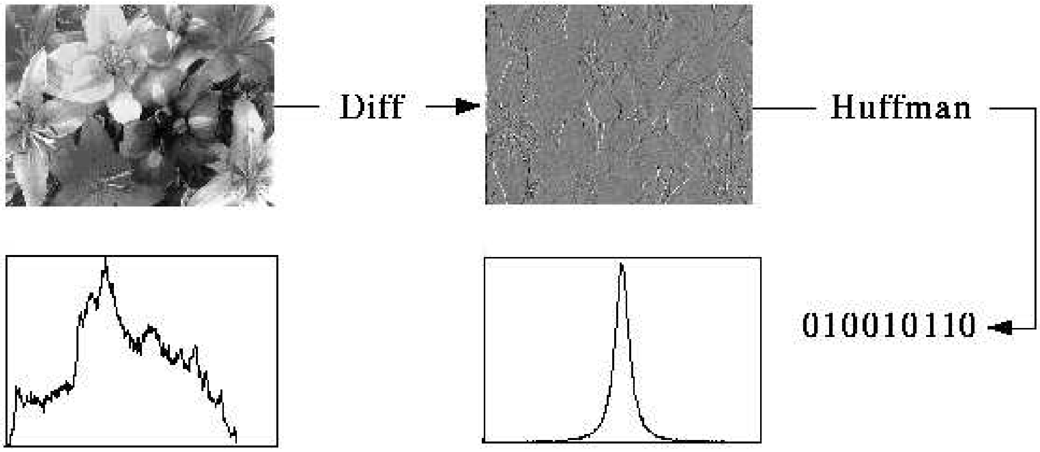
- Each image component is encoded in a single left-to-right, top-to-bottom scan.

  Baseline Sequential Mode, the one that we described above, is a simple case of the Sequential mode:
  - It supports only 8-bit images (not 12-bit images)
  - It uses only Huffman coding (not Arithmetic coding)

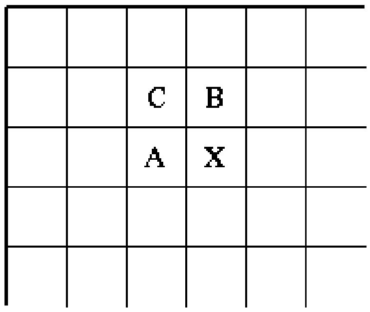
2. Lossless Mode

- A special case of the JPEG where indeed there is no loss.

Its block diagram is as below:



- It does not use DCT-based method! Instead, it uses a *predictive* method:
  A predictor combines the values of up to three neighboring pixels (not blocks as in the Sequential mode) as the predicted value for the current pixel, indicated by "X" in the figure below. The encoder then compares this prediction with the actual pixel value at the position "X", and encodes the difference losslessly.

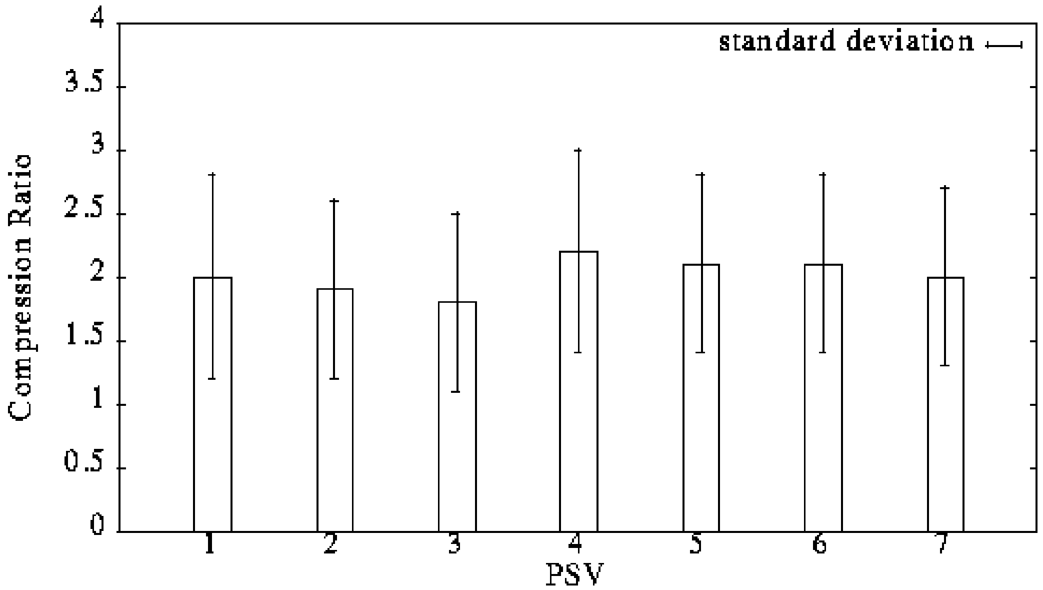


- It can use any one of the following seven predictors :

Predictor	Prediction
1	A
2	B
3	C
4	A + B - C
5	A + (B - C) / 2
6	B + (A - C) / 2
7	(A + B) / 2

Since it uses only previously encoded neighbors, the very first pixel I(0, 0) will have to use itself. Other pixels at the first row always use P1, at the first column always use P2.

- Effect of Predictor (test result with 20 images):



Note: "2D" predictors (4-7) always do better than "1D" predictors.

Comparison with Other Lossless Compression Programs (compression ratio):

```
 -------------------------------------------------------------------
       Compression Program             Compression Ratio
                               Lena   football    F-18   flowers
```

lossless JPEG	1.45	1.54	2.29	1.26
optimal lossless JPEG	1.49	1.67	2.71	1.33
compress (LZW)	0.86	1.24	2.21	0.87
gzip (Lempel-Ziv)	1.08	1.36	3.10	1.05
gzip -9 (optimal Lempel-Ziv)	1.08	1.36	3.13	1.05
pack (Huffman coding)	1.02	1.12	1.19	1.00

3. Progressive Mode

- Goal: display low quality image and successively improve.

- Two ways to successively improve image:

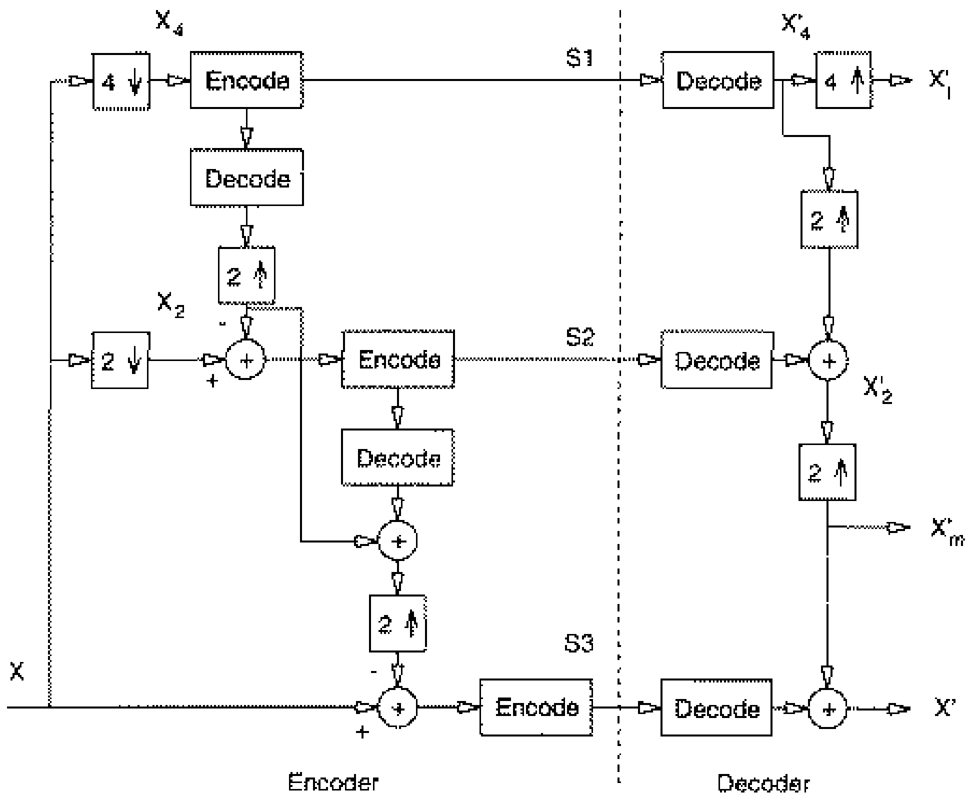
    1. *Spectral selection*: Send DC component and first few AC coefficients first, then gradually some more ACs.

    2. *Successive approximation*: send DCT coefficients MSB (most significant bit) to LSB (least significant bit).
    (Effectively, it is sending quantized DCT coefficients frist, and then the difference between the quantized and the non-quantized coefficients with finer quantization stepsize.)

4. Hierarchical Mode

A Three-level Hierarchical JPEG Encoder

(From *V. Bhaskaran and K. Konstantinides, "Image and Video Compression Standards: Algorithms and Architectures", 2nd ed., Kluwer Academic Publishers, 1997.*)



(a) Down-sample by factors of 2 in each dimension, e.g., reduce 640 x 480 to 320 x 240

(b) Code smaller image using another JPEG mode (Progressive, Sequential, or Lossless).

(c) Decode and up-sample encoded image

(d) Encode difference between the up-sampled and the original using Progressive, Sequential, or Lossless.

- Can be repeated multiple times.
- Good for viewing high resolution image on low resolution display.

4.2.5. JPEG 2000

- JPEG 2000 is the upcoming standard for Still Pictures (due Year 2000).
- Major change from the current JPEG is that wavelets will replace DCT as the means of transform coding.
- Among many things it will address:
  - Low bit-rate compression performance,

- Lossless and lossy compression in a single codestream,
- Transmission in noisy environment where bit-error is high,
- Application to both gray/color images and bi-level (text) imagery, natural imagery and computer generated imagery,
- Interface with MPEG-4,
- Content-based description.

Further Exploration

Try the Interactive JPEG examples and the JPEG examples.

Information about JPEG 2000.

Last Updated: ***11/3/99***